

# Energy, Exergy, and Economic Analyses and Optimization of Solar Organic Rankine Cycle with Multi-objective Particle Swarm Algorithm

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## Abstract

The high potential of solar energy in Iran as well as the problem of air pollution makes it increasingly inevitable that solar energy is used. In this work, the solar-powered organic Rankine cycle (ORC) is investigated. A solar-type collector is a flat plate collector. The energy, exergy, and economic analyses of the hybrid system with the MOPSO algorithm are carried out for Tehran, the capital of Iran. The working fluid of the solar collector is assumed to be water, and the working fluid of ORC is R123. The MATLAB software is used for the simulation, and to compute the R123 fluid properties, the Refprop software is used. The exergy investigation shows that the most exergy destruction is related to the evaporator. Two objective functions consisting of the exergy efficiency and the price of electricity are considered. The decision variables for this optimization are considered as the number of solar collector panels and the pumps, the turbine isentropic efficiency, and the pressures of the condenser and the evaporator. The Pareto diagram shows that the exergy efficiency of the system can vary in the range of 7.5-10.5 %, and the price of the produced electricity can vary in the range of 0.2-0.26 \$/kWh.

**Keywords:** Exergy, Organic Rankine cycle, Flat collector, Energy, Economic, Solar.

## 1. Introduction

The lack of fossil fuel and the gradual rise in its price as well as the environmental pollution and the increase in the global warming have caused the progress and usage of renewable energy as a major priority [1-3]. Among the solutions and technologies available in the renewable energy resources, the application of Organic Rankine Cycle (ORC) plays a significant role. The following benefits can be summarized for ORC [4-6]:

- The ORC technology is available to convert the low-temperature renewable energy resources such as geothermal, solar, and biomass into the electrical energy.
- Owing to the heat recovery of the waste heat generated in the industries, the need for energy can decrease affectedly.
- By applying ORC to the combined heating and power generation systems, a share of energy request for the buildings can be provided by these technologies.

- Application of solar ORC with absorption chiller (the hybrid system in this work) can supply all the electrical, heating, and cooling loads of a system by a minimum environmental impact and clean energy.

The shortage of fossil fuels, increasing the cost, and raising concerns about global warming are the major problems for fossil fuels. The solutions such as using the ORC technology powered by renewable energies are the key factors. The application of ORC to convert waste heat to useful power has been examined in different research works [7-9]. The usage and application of ORC systems have been conducted in some other studies [10, 11]. Numerous research works have been reported regarding the selection of the best working fluid in ORC [9,12].

Roy et al. [13] have examined the application of ORC with regenerator at the constant pressure and superheat condition for the two working fluids of R123 and R134. In this study, the efficiency, net output work of the turbine, overall irreversibility,

and second law efficiency of the cycle were obtained based on the constant and variable temperatures of the reservoir. As a result, the working fluid R123 was introduced as the best working fluid for this ORC.

Wang et al. [14] have optimized 13 different types of working fluids in ORC by the simulated annealing algorithm. In this study, the optimal parameters of ORC and the effects of the reservoir temperature, pinch temperature variations, and economic parameters on the ORC performance were also calculated. The results obtained revealed that the choice of working fluid had the highest effect on the performance of the cycle. Other similar research works have also been performed by the other researchers [15-17].

Moreover, the usage of different working fluids in ORC has been studied in other research works [18,19].

Also the application of the multi-component fluid for ORC has been examined [20-22]. Also the optimization of the multi-component working fluid has been performed [23,24].

Karellas et al. [25] have investigated the heat transfer performance of the supercritical fluid in the flat plate heat exchanger. They concluded that by increasing the efficiency of ORC, the cost of ORC was increased too.

Chen et al. [26] have compared R32 and CO<sub>2</sub> as the working fluids of ORC at the supercritical condition to convert low-temperature waste heat into useful power. The results obtained showed that although CO<sub>2</sub> was plentiful, inflammable, non-toxic, and cheap, the thermodynamic performance and operational pressure of this gas was poor in comparison with R32.

In another study, Chen et al. [27] have compared ORC with a Zeotropic mixture of 0.3 R32 and 0.7 R134a in the supercritical condition and pure R134 in the same conditions as the working fluid at the same temperature. The results obtained revealed that the efficiency of the zeotropic mixture as the working fluid varied from 10.8% to 13.3%.

Wang et al. [28] have examined the combined ORC and cooling systems, whereas R245fa as the working fluid of ORC and R134a was as the working fluid of the cooling system. In this combined system, these two systems were coupled by a shaft using a high efficiency microchannel and scroll expander heat exchanger. This configuration was designed with low weight and capacity to cool down an engine of the automobile.

Wang et al. [29] have analyzed the thermodynamic and optimal conditions of ORC

powered by the solar energy. The results of this study showed that this cycle by R245fa and R123 as the working fluid had a better efficiency.

Baccioli et al. [30] have investigated the solar parabolic collector and ORC in a dynamic model. The assessment performance of ORC over a year showed that this system had a good performance without a reservoir.

Bello and Tzivanidis [31] have examined ORC with the solar energy. The results obtained showed that based on 150-300 °C as the temperature of the resource and toluene as the working fluid, the amount of 400-880 kWh of electricity could be produced.

The cogeneration system with the application of ORC has been testified in several studies. Saadatfar et al. [32] have presented a system of combined power, heating, and cooling generation with solar energy using a nano-fluid as a working fluid. The results obtained showed that adding the nanoparticles of pentane silver to the working fluid was a suitable alternative as a working fluid. Mokhtari et al. [33] have investigated the hybrid systems of water treatment systems using reverse osmosis, parabolic trough solar collector, and ORC. This system was applied for the city of Mar Kola in the north of Iran. The fresh water produced by this system was about 4000 m<sup>3</sup>/day. Zhang et al. [34] have investigated a combination of the solar cycle and ORC to produce power, heating, and cooling of a residential place. The energy analysis of this combination was succeeded. The results obtained revealed that this combination fulfilled the needs of the case study during a year. Similar research works have been carried out by Patel et al. [35] and Mohammadi et al. [36]. Several types of research works exist in the literature about the cogeneration system with residential applications [37-41].

Based on the mentioned literature, it is clear that the feasibility study and optimization of solar ORC are a relatively novel idea.

In this research work, a combination of ORC and a flat plate solar collector was applied to generate electricity, heating, and cooling. In this study, the energy, exergy, and economic analyses of ORC with flat plate collectors were carried out. This study was done based on the weather and solar conditions in Tehran. By considering the decision variables, the optimization of two functions consisting of electricity cost and exergy efficiency was carried out based on the MOPSO algorithm.

The innovations of this article are as follow:

- Feasibility study of the application of solar ORC for Tehran (Iran) based on the energy, exergy, and economic analyses;

- Two-objective (exergy and electricity cost) optimization of ORC performed by the MOPSO algorithm;
- Sensitivity analysis of the ORC system based on different decision variables.

**2. Mathematical modeling**

A schematic representation of the system is shown in figure 1.

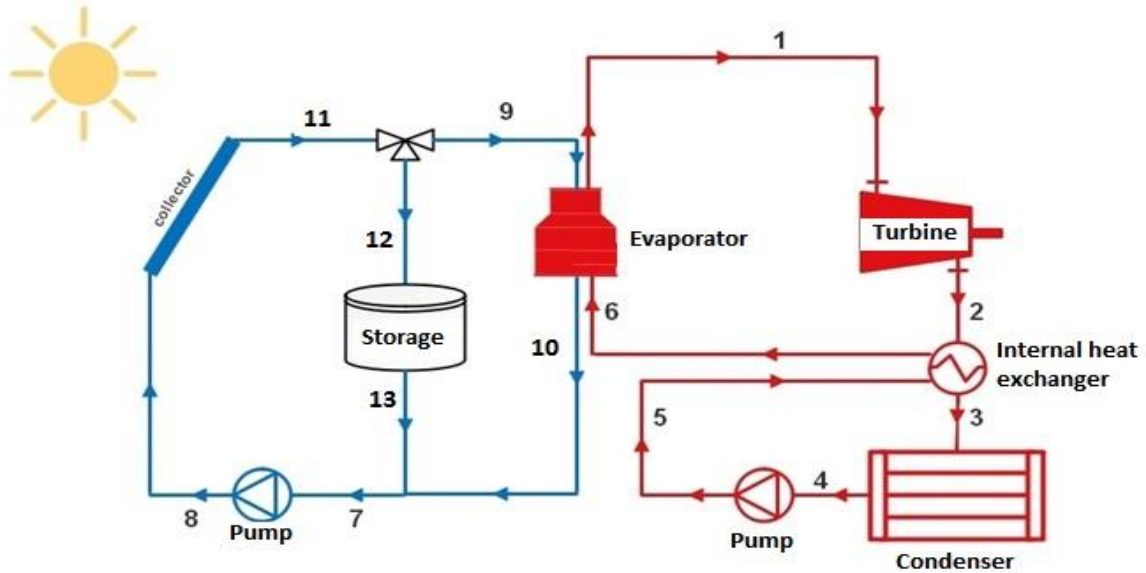


Figure 1. A schematic diagram of the case study.

As shown in this figure, the absorbed energy by the sun enters an intermediate fluid (water), and then this energy is transferred to the operational fluid at the evaporator of ORC. In ORC, the working fluid of ORC in a superheat condition enters the turbine or expander (point 1). Thus the energy is transferred to the shaft, and a power is produced. Then the working fluid can come out of the turbine in a superheat state (point 2). This working fluid passes through a heat exchanger as a regenerator, and the heat is taken from this part and transferred to the operational fluid, entering the evaporator. Thus the working fluid leaves the regenerator in a saturated vapor (point 3). Then this fluid passes through the condenser, losses the heat, and leaves the condenser as a saturated liquid. Thus by passing through the pump, the pressure of the working fluid rises. Then it enters the internal heat exchanger (regenerator), and the working fluid heats up by taking heat from the extracted fluid of the turbine. As a result, its

temperature is increased, and hence, the efficiency of the system is increased too. Finally, this ORC working fluid enters the evaporator to gain heat from the intermediate fluid flow of the solar collector. Therefore, this cycle is repeated over time.

The case study of this research work was Tehran. The city is extended in the longitudinal ranges of 51 degrees and 2 minutes, eastern to 51 degrees and 36 minutes, and eastern over 50 km. Its latitude ranges from 35 degrees and 35 minutes of the north to 35 degrees and 50 minutes over 30 km. The temperature of the environment was determined as one of the decision variable parameters during the day and in the different months according to the reference. The average monthly ambient temperature and wind speed of Tehran are given in table 1 for different months [42].

An important parameter in a solar energy system is the solar radiation (Figure 2). Based on the

Table 1. Daily average temperature of Tehran from 1951 to 2010 for different months.

Months	Jan	Feb	Mar	Apr	May	June	Jul	Aug	Sep	Oct	Nov	Dec
Temp (°C)	8.3	6.0	10.7	16.8	22.1	27.5	30.3	29.5	25.5	19.0	11.6	5.9
Wind speed (m/s)	4.5	5.2	5	5.6	5.9	5.4	4.5	4	3.8	4.2	4.8	3.6

reference [24], the amount of the radiation intensity in Tehran can be observed over a year.

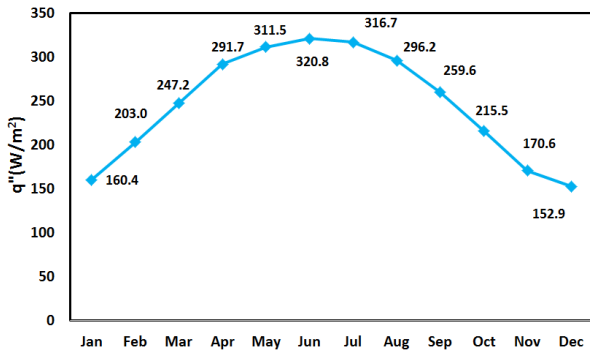


Figure 2. Average solar radiation in Tehran over a year [24].

The specifications of a solar flat collector and storage tank are shown in table 2.

Table 2. Specifications of a solar flat collector.

No.	Specification	Unit	Value
1	Length of flat plate solar collector	m	1.57
2	Width of flat plate solar collector	m	0.8
3	Number of pipes	-	80
4	Diameter of pipes	m	0.127
5	Storage tank volume	m <sup>3</sup>	1
6	$\epsilon_p$	-	0.96
7	$\epsilon_a$	-	0.96

The rate of the absorbed energy by the solar flat plate collector is obtained by the following equations [43]:

$$S = I_b R_b (\tau\alpha)_b + I_d (\tau\alpha)_d \frac{(1 + \cos \beta)}{2} + (I_b + I_d) (\tau\alpha)_g \rho_g \frac{(1 + \cos \beta)}{2} \quad (1)$$

In equation (1), the indices b, d, and g are due to the direct radiation, scattered radiation from the sky, and scattered radiation due to the reflection of the ground surface. I is the intensity of radiation on the horizontal surface by considering the effect of the environment dust, which is calculated based on the Reference [44].

The constant values that are determined by the experimental results are multiplied by the amount of radiation intensity, and ultimately, the amount of these quantities is determined. Moreover,  $\tau\alpha$  is the transmission absorption coefficient,  $\beta$  is the solar collector slope, and  $\rho_g$  is the reflection coefficient of the Earth's surface that it is equal to 0.93.  $R_b$  is a dimensionless parameter, and represents the scattered radiation of the sky, and is expressed as follows [43,44]:

$$R_b = \frac{\cos \theta}{\cos \beta} \quad (2)$$

In this case,  $\theta$  is the angle of the sunlight with the collector surface. The scattered radiation is calculated as follows [43]:

$$\frac{I_d}{I_t} = \begin{cases} 1 - 0.09k_T k_T < 0.22 \\ 0.9511 - 0.1604k_T + 4.388k_T^2 & 0.22 < k_T < 0.8 \\ -16.638k_T^2 + 12.336k_T^4 \\ 0.165k_T > 0.8 \end{cases} \quad (3)$$

In this case,  $k_T$  is dimensionless, and is the average monthly clearance coefficient.

The general heat loss of the collector is obtained by the following equation [43]:

$$\dot{Q}_{Loss} = U_L A (T_p - T_a) \quad (4)$$

In the above equation,  $U_L$  is the total heat transfer coefficient, A is the collector area, and  $T_a$  is the ambient temperature. In order to obtain the total heat transfer coefficient, the following relationship exists [43]:

$$U_L = U_t + U_b + U_e \quad (5)$$

$U_e$  and  $U_b$  are the total heat transfer from the sides and the bottom, respectively, and  $U_t$  is the overall heat transfer coefficient from above the collector, which is calculated by the following equation [43].

$$U_t = \frac{C}{T_p} \left( \frac{T_p - T_a}{1 + f} \right)^{0.33} + \frac{1}{h_w} + \frac{\sigma(T_p^2 + T_a^2)(T_p + T_a)}{\frac{1}{\epsilon_p} + 0.05(1 + \epsilon_p) + \frac{1 + f}{\epsilon_c} - 1} \quad (6)$$

In the above equation,  $h_w = 2.6 + 3V_{wind}$  is the forced heat transfer coefficient between the glass cover exposed to ambient air, which is determined in terms of wind speed ( $V_{wind}$ ). Also  $\epsilon_p$  and  $\epsilon_c$  are the diffusion coefficients for the absorption plate and the glass cover for infrared radiation, respectively. Also  $\sigma$  is the Stephen Boltzmann's constant. The parameters C and f are calculated by the following equations [43]:

$$C = 365.9(1 - 0.00883\beta + 0.0001298\beta) \quad (7)$$

$$f = 1.091(1 - 0.04h_w + 0.0005h_w) \quad (8)$$

$\beta$  is the solar collector slope. The amounts of  $U_e$  and  $U_b$  are calculated as follow [43]:

$$U_b = \frac{k_b}{L_b} \quad (9)$$

$$U_e = \frac{k_e}{L_e} \quad (10)$$

In the above equations,  $L_b$  and  $k_b$  are the width

and thermal conductivity coefficients of the insulation plate located below the absorbent plate, respectively. Also  $Le$  and  $k_e$  are the thickness and thermal conductivity coefficient insulation plate that is located on the sides of the absorbent plate. The useful heat gain rate and plate temperature are calculated by the following equations [43]:

$$\dot{Q}_{SC} = AF_R(I_t(\tau\alpha) - U_L(T_i - T_a)) \quad (11)$$

$$T_p = T_i + \frac{\dot{Q}_{SC}}{AF_R U_L} (1 - F_R) \quad (12)$$

$I_t$ ,  $\tau\alpha$ ,  $T_i$ , and  $A$  are the direct radiation flux on the slope plate, transmission absorption coefficient, temperature of the fluid to the collector, and collector area, respectively. Also,  $F_R$  is the harvesting factor of the collector, and it is calculated by the following equation [43]:

$$F_R = \frac{\dot{m}C_p}{AU_L} \left[ 1 - e^{-\left(\frac{U_L F' A}{\dot{m}C_p}\right)} \right] \quad (13)$$

In this equation,  $\dot{m}$  and  $C_p$  are the mass flow rates of water entering the collector and specific heat at a constant pressure of water, respectively. Also  $F'$  is an efficiency coefficient of the collector, which is calculated by the following equation [43]:

$$F' = \frac{\frac{1}{U_L}}{W \left[ \frac{1}{U_L(D_o + W - D_o)F} + \frac{1}{C_b} + \frac{1}{\pi D_i h_{fi}} \right]} \quad (14)$$

In the above relation,  $W$ ,  $D_i$ , and  $D_o$  are the distance between the pipes in the collector, inner diameter, and outer diameter of the fluid tube. Also  $C_b = 0.027$  and  $h_{fi}$  are the conduction coefficients of the substances that connect the tube to the absorber plate and the heat transfer coefficient of fluid, respectively. The last parameter is calculated according to the Chininskian relation[45]. The energy conservation equations for ORC are in table 3[45].

**Table 3. Conservation of energy equation energy and exergy for ORC.**

No.	Equipment	Energy Equation
1	Pump	$\dot{W}_p = \dot{m}_1(h_5 - h_4)$
2	Evaporator	$\dot{Q}_E = \dot{m}_5(h_1 - h_6)$
3	Condenser	$\dot{Q}_C = \dot{m}_1(h_3 - h_4)$
4	Internal heat exchanger	$\dot{Q}_{IHE} = \dot{m}_2(h_3 - h_2) = \dot{m}_5(h_6 - h_5)$
5	Turbine	$\dot{w}_T = \dot{m}_1(h_1 - h_2)$

In the table above,  $\dot{m}$  is the fluid mass flow rate,  $\dot{W}$  and  $\dot{Q}$  are the rates of output work and heat transfer, respectively, and  $h$  (J/kg) is the enthalpy. Also the sub-titles P, T, C, E, and IHE represent the pump, turbine, condenser, evaporator, and internal heat exchanger, respectively. The points

are also shown in figure 1.

Also the heat transfer rate of the solar collector can be obtained by the following equation [45]:

$$\dot{Q} = U \cdot A \cdot LMTD \quad (15)$$

where  $U$ ,  $A$ , and  $LMTD$  are the heat transfer coefficient, area of the heat exchanger, and logarithmic mean temperature difference, respectively [45].

The logarithmic mean temperature difference is defined as:

$$LMTD = \frac{\Delta T_A - \Delta T_B}{\ln\left(\frac{\Delta T_A}{\Delta T_B}\right)} \quad (16)$$

In this model, the reservoir tank is a storage tank with water fluid. The returned fluid from the collector and the fluid entering from the hot water are completely mixed. The heat loss of the storage tank is calculated based on the defined efficiency ( $\eta_{TST}$ ) by the Reference [46].

Therefore, by uniformly assuming the fluid temperature in the tank and neglecting the potential and kinetic energy, the energy conservation to the storage tank is calculated as follows [46]:

$$mC_p \frac{dT}{dt} = \eta_{TST}(\dot{Q}_{net}) \quad (17)$$

where  $T$  is the mean temperature of the storage tank,  $m$  is the stored mass inside the tank,  $t$  represents the time, and  $\dot{Q}_{net}$  is the net heat transfer of the tank.

Exergy can be separated into four parts. The physical exergy and chemical exergy are two important types of exergy. In this work, the two components of kinetic exergy and potential exergy are neglected. By application of the first and second laws of thermodynamics, the following exergy equilibrium is found [47-50]:

$$\dot{E}x_Q + \sum_i \dot{m}_i ex_i = \sum_e \dot{m}_e ex_e + \dot{E}x_W + \dot{E}x_D \quad (18)$$

where  $\dot{E}x_Q$ ,  $\dot{m}_i$ , and  $ex_i$  are the heat transfer exergy flow, inlet mass flow rate, and specific exergy for  $i$  stream. Also  $\dot{m}_e$ ,  $ex_e$ ,  $\dot{E}x_W$ , and  $\dot{E}x_D$  are the outlet mass flow rate and specific exergy, exergy flows of the work, and rate of exergy destruction, respectively.

The physical exergy of a stream  $i$  is defined as follows [51,47].

$$ex = (h_i - h_0) - T_0(s_i - s_0) \quad (19)$$

In the above equation,  $ex$ ,  $h_i$ ,  $h_0$ ,  $T_0$ ,  $s_i$ , and  $s_0$  are the specific exergy, inlet enthalpy of the enthalpy of fluid at reference conditions, ambient

temperature, entropy of stream *i*, and entropy at the reference condition, respectively. Table 4 shows the exergy balance equation for various components of a cycle.

**Table 4. Exergy balance equations for various cyclic components.**

No.	Equipment	Exergy Equation
1	Pump	$\dot{m}_1(ex_5 - ex_4) + \dot{W}_P$
2	Evaporator	$\left( \left( 1 - \frac{T_0}{T_E} \right) \dot{Q}_E + \dot{m}_6 ex_6 \right) \left( 1 - \frac{T_0}{T_E} \right) \dot{Q}_E + \dot{m}_1 ex_1 - \dot{m}_6 ex_6$
3	Condenser	$\left( 1 - \frac{T_0}{T_C} \right) \dot{Q}_C + \dot{m}_3 ex_3 - \dot{m}_4 ex_4$
4	Internal heat exchanger	$T_0 [\dot{m}_5(ex_6 - ex_5) + \dot{m}_2(ex_3 - ex_2)]$
5	Turbine	$T_0 \dot{m}_1(ex_1 - ex_2) - \dot{W}_T$
6	Solar Collector	$I_g \times A \left[ 1 + \frac{1}{3} \left( \frac{T_a}{T_{sun}} \right)^4 - \frac{4}{3} \left( \frac{T_a}{T_{sun}} \right) \right]$

In the table above,  $T_E(K)$  and  $T_C(K)$  are the evaporator and condenser temperatures, respectively.  $T_{sun}$  is the sun temperature of 6,000 (K), and  $T_{ambn}(K)$  is the ambient temperature. The first and second efficiencies based on the thermodynamic laws are calculated by the subsequent relationships:

$$\eta_I = \frac{\dot{W}_T - \dot{W}_P}{\dot{Q}_E} \quad (20)$$

$$\eta_{II} = \frac{\dot{W}_T - \dot{W}_P}{I_g \times A \left[ 1 + \frac{1}{3} \left( \frac{T_a}{T_{sun}} \right)^4 - \frac{4}{3} \left( \frac{T_a}{T_{sun}} \right) \right]} \quad (21)$$

The price of the produced electricity for the cycle is calculated by [52]:

$$C_E = \frac{CI \frac{i(1+i)^L}{(1+i)^L - 1} + C_{OM}}{8760(\dot{W}_T - \dot{W}_P)} \quad (22)$$

**Table 6. Characteristics of working fluid of ORC.**

GWP (100 year)	ODP	ALT (year)	Safety degree ASHRAE	Critical Pressure (MPa)	Critical Temperature (K)	Boiling point (K)	Molecular mass ( $\frac{kg}{kmol}$ )	Fluid
77	0.02	1.3	B1	3.662	456.83	300.97	152.93	R123

In the above equation, *C* is the initial installation

### 3. Multi-objective particle swarm optimization algorithm

The bird migration algorithm is a set of optimization algorithms that operate based on the random population generation. In this algorithm, the behavior of a massive group of birds or groups of fish is simulated [57-60].

Every member (particle) of this group is defined by the position vectors and velocity vector in a search space. In each iteration, the new position of

cost, *L* is the equipment lifetime in terms of year, and *i* is the interest rate. The maintenance and operation costs are 4% of the initial installment cost.

The price functions of the main equipment can be calculated from table 5 [53-55].

**Table 5. Cost of purchase and installation of different cycle equipment**

Equipment Name	Unit	Cost function
Turbine	\$	$2237(\dot{w}_T)^{0.41}$
Pump	\$	$1026 \left( \frac{\dot{W}_P}{300} \right)^{0.25}$
Condenser	\$	0338.6 A
Evaporator	\$	216.6+353.4A
Solar collector	\$/m <sup>2</sup>	355

The characteristics of the working fluid are shown in table 6 [56]. The working fluid in this research work is R123. The positivity of the slope in R123 makes it possible to reduce the pressure of the condenser. In this manner, a two-phase flow cannot be produced, so there is no damage to the turbine. As a result, there is no need to superheat the fluid, resulting in low cost for evaporator due to reducing the size of the heat exchanger. For dry fluids with a positive gradient of saturated vapor curve, IHE can be used to increase the cycle efficiency. This consideration was assumed in this research work. As the pressure of the condenser is higher than the atmospheric pressure, it reduces the costs, and an ejector is not required. A higher pressure than the atmospheric pressure prevents air leakage into the system, and there is no escaping of R123 by good sealing. The low pressure of the evaporator in comparison with water is another feature of using R123, which reduces the complexity of the system. The chemical stability at high temperatures is another characteristic of using R123 as a working fluid.

the particles is defined based on the position and velocity vectors in a search space.

At each time interval, the new position of each particle is found based on the current velocity vector. Also the new position of all particle and the best position of the best particle in the group in the search domain are updated every time [57-59].

The algorithm is initially defined for the continuous and discrete parameters. This

algorithm is extended to a discrete state condition. This algorithm is also used for one or several objective functions [57-59]. Figure 3 shows a flowchart of the bird migration algorithm [61].

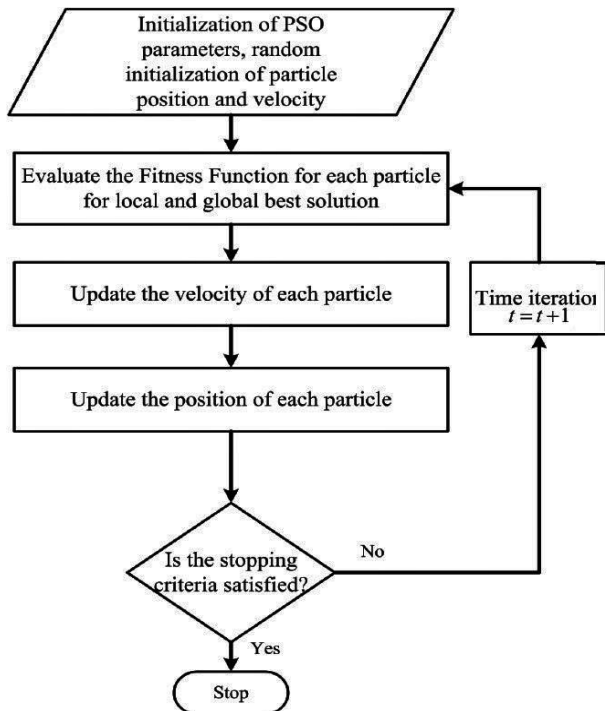


Figure 3. A bird migration algorithm flowchart.

#### 4. Results and Discussion

In this research work, a program was written in the MATLAB software. The Refprop software was used to calculate the fluid properties. The results obtained from this work were compared with the results of the Reference [62] for validation. In this comparison, the cycle of that reference was simulated, and the results were compared. Tables 7 and 8 show the results of this comparison. Table 9 shows the values of the thermodynamic properties at different points in the cycle. The optimization process was carried out between the upper and lower limits of the variables of the cycle. The limitation of these variables is shown in table 10.

The objective function of optimization is as follows:

$$C_E \& \eta_{II} \quad [23]$$

Figure 4 represents the Pareto chart.

As it can be seen in this figure, three points are highlighted on the Pareto graph, shown as A, B, and C. Point A has the lowest electricity price and exergy efficiency, whereas point B has an average value of electricity price and exergy efficiency. Finally, point C has the highest electricity price and exergy efficiency. The other values for the points A, B, and C are presented in table 11.

Figure 5 shows the variation in the exergy and thermal efficiencies of ORC in terms of the pressure of the evaporator. As it can be seen in the figure, by increasing the pressure of the evaporator, the exergy and thermal efficiencies are increased. The exergy destruction and net produced power by ORC are shown in figure 6. Comparison of these two figures show, as the exergy destruction of the cycle is decreased, the exergy efficiency of the cycle is increased. It is also possible to observe that the cycle thermal efficiency is improved by taking the heat and increasing power production. Increasing the pressure due to the saturation state at the entrance of the turbine causes an increase in the temperature. The limiting input of hot water is one of the basic constraints in determining the pressure of the evaporator.

Figure 7 shows the exergy destruction for each component versus the evaporator pressure. It can be observed that the evaporator and condenser components have the highest exergy destruction. This is due to the entropy generation caused by the temperature difference between the hot and cold flows.

Figure 8 shows the exergy efficiency of each component. It can be observed that the two components have the highest exergy destructions, and have the lowest exergy efficiencies.

One of the economic parameters is the total annual cost for each equipment. This parameter is obtained by adding the sum of the normalized and utilization costs. The normalized cost is the cost of the equipment that is divided over the useful life of the equipment. Figure 9 shows the variation in this parameter in terms of the evaporator pressure. As the temperature of the absorbed heat in the evaporator increases, the cost of this equipment is increased too. Moreover, by increasing the pressure and temperature of the fluid flow at the turbine entrance, the cost of this equipment is increased. It can be concluded that as the evaporator pressure increases, the cost and efficiency are increased too.

Another important parameter is the pressure of the condenser, which plays a crucial character in the cycle efficiency as well as the power generation. In the cycles that deal with water and steam, the pressure of the condenser is an important parameter in increasing the lifetime of the turbine. In ORC with dry fluids, as it is stated, the turbine output is in the superheat section. As a result, this parameter can be reduced but the limitation of the cold thermal source is one of the constraints governing the condenser pressure.

In most organic fluids, which are used as refrigerants by reduction of the pressure, causes temperature reduction. Thus it requires a lower thermal resource to condense the desired fluid. As the pressure of the condenser increases, the power of the system is reduced. Thus it directly affects the exergy efficiency of the entire system, and leads to its reduction. This cycle is used just for

power generation so that the exergy efficiency of the whole cycle is in agreement with the exergy efficiency of ORC. It should be noted that lower condenser temperatures are caused by lower condenser pressures (see figure 10). The reduction of the inlet temperature throughout the evaporator causes the rise of the heat absorption.

**Table 7. Energy and exergy validation for this research work with Reference [62].**

Points	T (°C)		Error (%)	P (MPa)		Error (%)	ex (kJ/kg)		Error (%)
	Present study	Safarian		Present work	Safarian		Present work	Safarian	
1	25	25	0	0.044	0.048	9.0	0	0	0
2	25	26.1	4.4	2.5	2.5	0	1.84	1.77	3.8
3	50.78	55	8.3	2.5	2.5	0	3.7	4.14	9.8
4	193.67	195	0.6	2.5	2.5	0	63.28	64.02	1.1
5	85.1	92	8.1	0.044	0.048	9.0	4.7	5.08	8.0
6	52.28	56	7.1	0.044	0.048	9.0	1.6	1.73	8.-

**Table 8. Comparison of some important parameters of this research work with Reference [62].**

Parameter	Unit	Present work	Safarian [62]
Evaporator heat transfer	kW	252	252
Condenser heat transfer	kW	188	196
Turbine power generation	kW	54.4	56.5
Pump power generation	kW	2.00	1.2
Net power	kW	52.37	54.3
Thermal efficiency	%	20.78	21.5
Mass flow rate (organic fluid)	kg/s	1.10	1.15

**Table 9. Energy and exergy values at different points of the cycle.**

Point	T (°C)	P(kPa)	x	h (kJ/kg)	s (kJ/kg.K)	Ex (kW)
1	72.15	400	1	426.5	1.681	23.89
2	48.32	150	1>	413.4	1.691	15.54
3	39.08	150	1	406.6	1.67	15.31
4	39.08	150	0	240.9	1.139	11.41
5	39.22	400	0	241.1	1.14	11.5
6	45.67	400	0	248	1.161	11.71
7	67.78	150	0	283.7	0.9277	11.84
8	67.78	200	0	283.7	0.9277	11.84
9	89.88	150	0	376.4	1.191	26.07
Water in	25	100	0	104.8	0.367	0
Water out	35	100	0	146.6	0.505	1.455

**Table 10. Upper and lower bounds of variables.**

Parameter	Lower bound	Upper bound
P <sub>E</sub> (kPa)	300	560
P <sub>C</sub> (kPa)	145	210
Number of collector units (1.2 m <sup>2</sup> )	100	300
Turbine isentropic efficiency	70	90
Pump isentropic efficiency	70	90



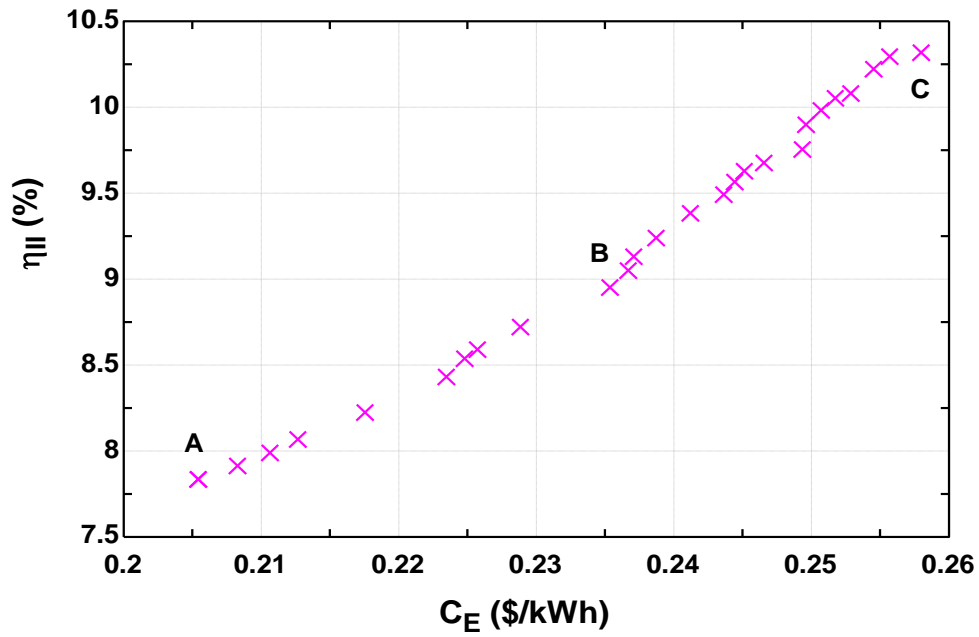


Figure 4. Pareto graph for the objective functions of exergy efficiency and the electricity price.

Table 11. Values for different variables and objective functions for points A, B, and C.

Parameter	A	B	C
$P_E$ (kPa)	425	424.6	424.0
$P_C$ (kPa)	145.6	145.62	145.14
Number of collector units (1.2 m <sup>2</sup> )	247	155	111
Turbine isentropic efficiency	88.8	88.54	88.98
Pump isentropic efficiency	88.8	85.6	82.0
$\eta_I$ (%)	8.42	8.36	8.39
$\eta_{II}$ (%)	7.83	8.95	10.29
$C_E$ (\$/kWh)	0.2054	0.2353	0.2557

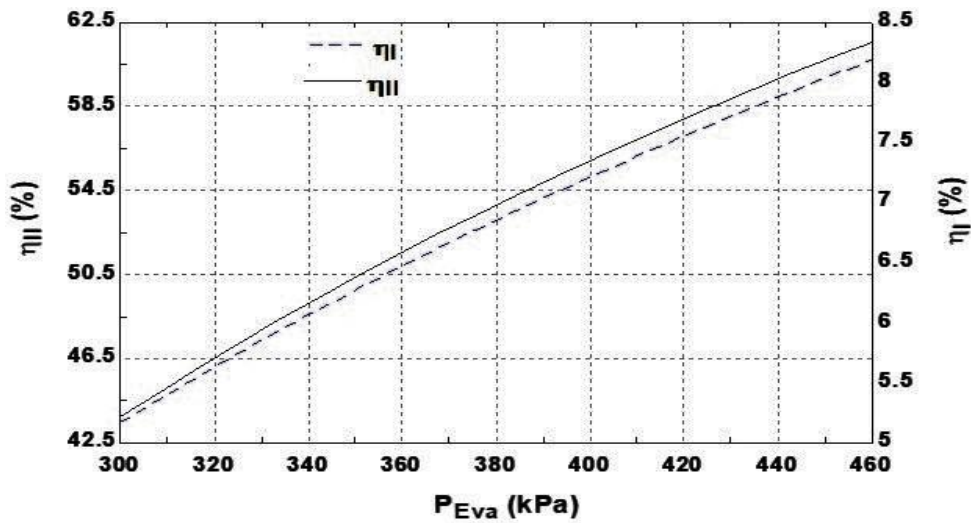


Figure 5. Changes in the energy and exergy efficiencies of ORC versus the evaporator pressure.

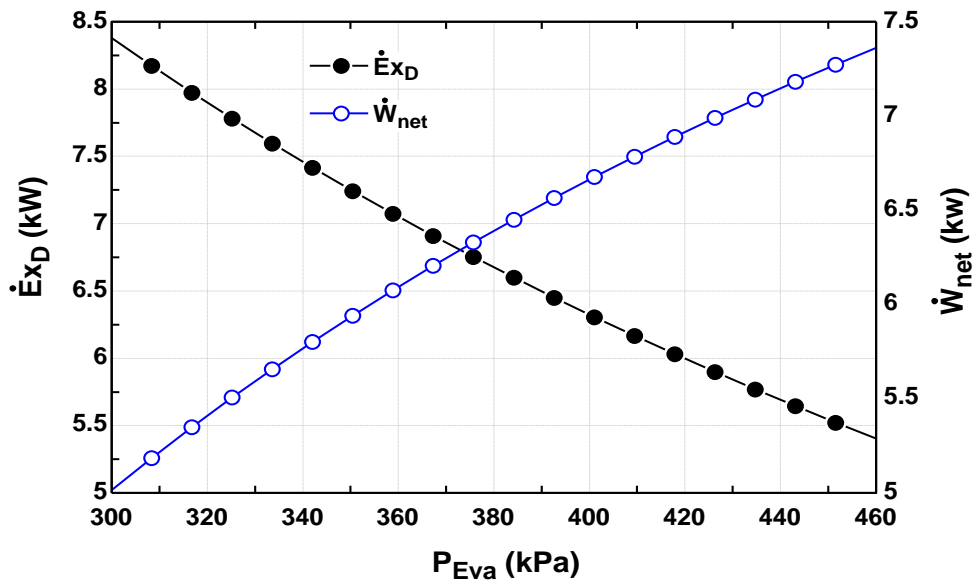


Figure 6. Changes in the exergy destruction and net produced power by ORC based on the evaporator pressure.

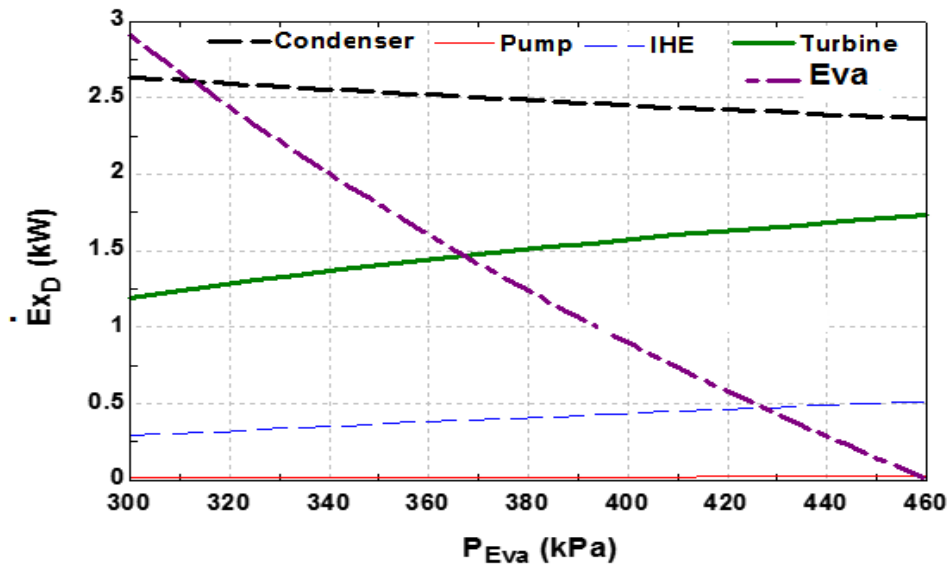


Figure 7. Changes in the exergy destruction for the ORC components based on the pressure evaporator.

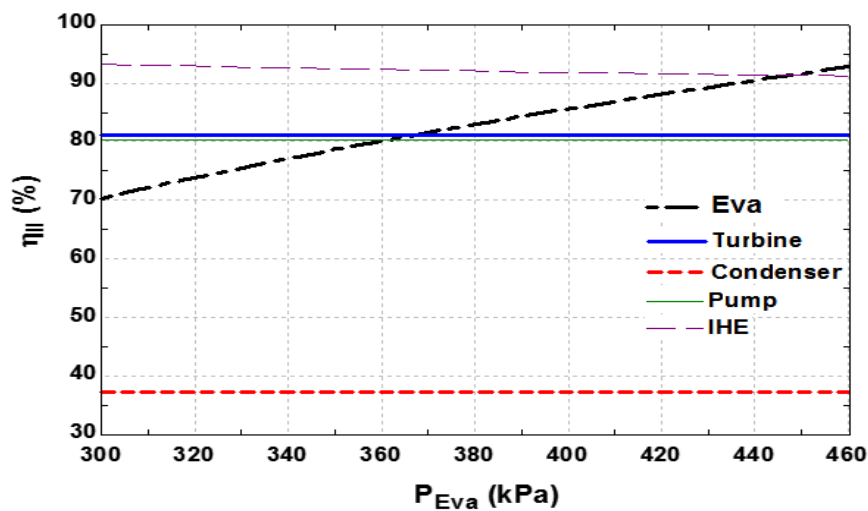


Figure 8. Exergy efficiency changes of any ORC component based on the evaporator pressure.

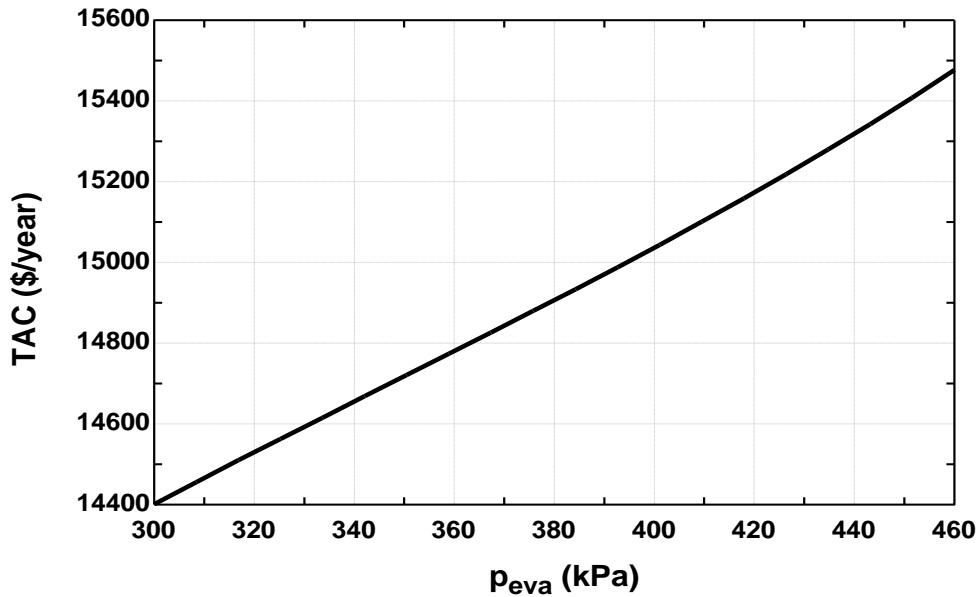


Figure 9. Changes in the total annual cost of the system with variation in the evaporator pressure.

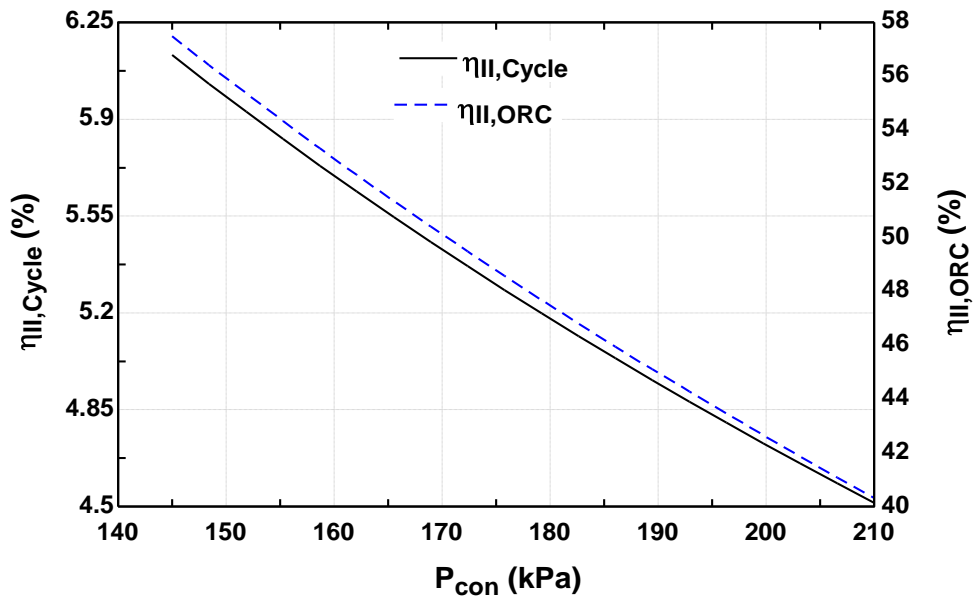


Figure 10. Changes in the total cycle and ORC exergy efficiencies.

### 5. Conclusion

In this research work, the application of a solar ORC with an absorption chiller to supply all energy needs (electrical, heating, and cooling) were examined. In order to comply with this goal, the energy, exergy, and economic simulations of this cycle were investigated. In the meantime, the MOPSO algorithm was applied for optimization of the purposes. In the optimization of this cycle, two objective functions consisting of exergy efficiency and electricity price were examined. In the meantime, the number of variables such as the number of solar panels, isentropic efficiencies of pump and turbine, condenser, and evaporator pressures was considered as a decision variable.

The optimization results revealed that by increasing the exergy efficiency from 7.5% to 10.5%, the price of the produced electricity increased from 0.2 to 0.26 \$/kWh.

The major findings of this work are as follow:

- Application of the solar ORC cycle with absorption chiller (the hybrid system in this work) can supply all the electrical, heating, and cooling loads of a system by a minimum environmental impact and clean (solar) energy;
- Two objective functions consisting of the exergy efficiency and electricity price were plotted on a Pareto-front graph in

order to find out three alternatives (highest, lowest, and medium values for the electricity price and exergy efficiency);

- The pressures of the evaporator and the condenser play an important role in the optimization of the solar ORC;
- The maximum exergy destruction rate is in the evaporator;
- For the future research works, the hydrogen and syngas production of this system by choosing the methanation plant can be used to meet the thermal energy needs of the residential building.

### Abbreviations and Notations

MOPSO	Multi-objective particle swarm optimization
ORC	Organic Rankin cycle
TAC	Total annual cost

### Nomenclatures

A	Surface area of collector (m <sup>2</sup> )
c <sub>p</sub>	Specific heat at a constant pressure (J/kg K)
C	Cost (\$), specific parameter in equation (7)
C <sub>b</sub>	Constant parameter (-)
D <sub>o</sub>	Tube outside diameter (m)
D <sub>i</sub>	Tube inside diameter (m)
ex <sub>i</sub>	Specific exergy (J/kg)
Ė <sub>x</sub>	Exergy rate (W)
f	Specific parameter in equation (8)
F <sub>R</sub>	Harvesting factor of the collector (-)
F'	Efficiency coefficient of the collector (-)
h	Specific enthalpy (J/kg)
h <sub>w</sub>	Forced heat transfer coefficient (-)
h <sub>fi</sub>	Heat transfer coefficient of fluid inside Tube (W.m <sup>-1</sup> .k <sup>-1</sup> )
i	Interest rate (-), inlet in equation (11)
I	Intensity of radiation (W/m <sup>2</sup> )
K	Thermal conductivity (W.m <sup>-1</sup> .K <sup>-1</sup> )
k <sub>T</sub>	Average monthly clearance coefficient (-)
L	Thickness or width (m), equipment lifetime (Year)
ṁ	Mass flow rate (kg/s)
m	Mass (kg)
Q̇	Heat transfer rate (W)
R <sub>b</sub>	Scattered radiation of the sky (-)
S	Specific entropy(J/kg.K), rate of

	absorbed energy(W/m <sup>2</sup> ) equation (1)
t	Time (s)
T	Temperature (°C) or (K)
U	Heat transfer coefficient (W.m <sup>-2</sup> .K <sup>-1</sup> )
V	Velocity (m/s)
W	Distance between riser tubes (m)
Ẇ	Power (W)

### Subscripts

A	Ambient
B	Back
b	Below or bottom (absorbent plate)
B	Beam
C	Condenser, specific parameter in Equation (7), cost (\$) in equation (22)
D	Diffusion
d	Scattered radiation from the sky
D	Destruction
e	Sides (absorbent plate)
E	Evaporator
f	Specific parameter in equation (8)
g	Scattered radiation from the ground
H	Hot fluid
h <sub>w</sub>	Forced heat transfer coefficient
IHE	Internal heat exchanger
L	Loss, life time (year) in equation (22)
P	Pump
sun	Sun
t	Total
T	Turbine
wind	Wind

### Greek symbols

τ <sub>a</sub>	Transmittance-absorptance product (-)
η	Efficiency (-)
α	Absorber coefficient (-)
β	Solar collector slope (rad)
ρ <sub>g</sub>	Reflection coefficient of the Earth's surface, which is equal to 0.93
ε <sub>g</sub>	Emissivity of glass covers (-)
ε <sub>p</sub>	Absorber plate emittance (-)
σ	Stefan-Boltzmann constant (= 5.67 × 10 <sup>-8</sup> W/m <sup>2</sup> K <sup>4</sup> )
Θ	Angle of sunlight incidence (rad)

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